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### 3. Fault Location Algorithms

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### Fault Location Overview

- Traditional Methods of determining the location of a fault on T&D lines
  - Impedance Approaches (Our Focus)
  - Traveling Wave Approaches
  - Problems in Distribution Network
- Other Methods
  - Short-circuit analysis software
  - Customer calls (distribution case)
  - Line inspection
  - Fault Indicators (4)
- New Opportunities
  - Smart Sensors (6)
  - Smart Meters (6)

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### Impedance-Based Measurement Technique Overview

- Calculation of the fault location from the apparent impedance seen looking into the line from one end (or two ends).
- Steady-State Approach
- Phase-to-ground voltages and current in each phase must be determined.
- Fault Impedance Influence
- Loading Influence
- Ground Fault Case
  - Zero-sequence Impedance Information
  - Ground Compensation Factor

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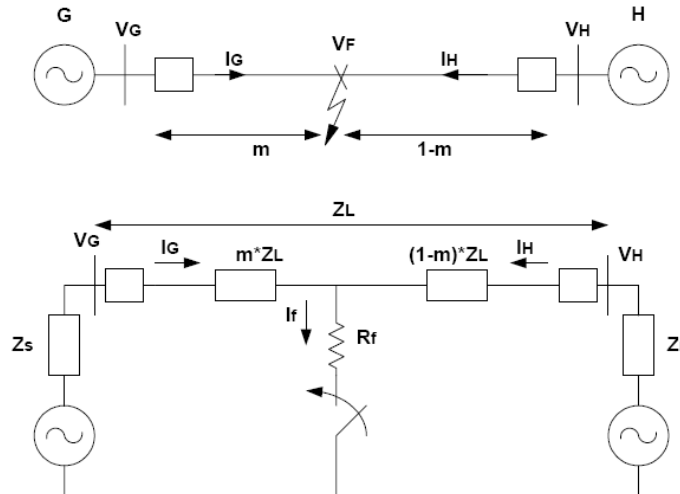
### Simple Impedance Equations (with $R_f = 0$ )

Fault Type	Positive-Sequence Impedance Equation ( $m \cdot Z_{1L} =$ )
A – Ground	$V_A / (I_A + k \cdot I_R)$
B – Ground	$V_B / (I_B + k \cdot I_R)$
C – Ground	$V_C / (I_C + k \cdot I_R)$
A-B or A-B-G	$V_{AB} / I_{AB}$
B-C or B-C-G	$V_{BC} / I_{BC}$
C-A or C-A-G	$V_{CA} / I_{CA}$
A-B-C	Any of the following: $V_{AB}/I_{AB}$ , $V_{BC}/I_{BC}$ , $V_{CA}/I_{CA}$

- $k = (Z_{0L} - Z_{1L}) / (3 \cdot Z_{1L})$  ground compensation factor
- $Z_{0L}$ : zero-sequence line impedance
- $m$ : per unit distance to fault
- $I_R$ : Residual Current

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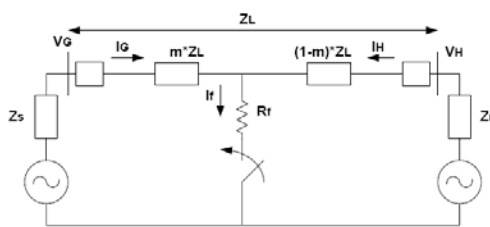
## Basic Model with System Parameters



- Simplified transmission line with two sources

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## Impedance (Distance) Equation



$$V_G = m \cdot Z_L \cdot I_G + R_f \cdot I_f$$

$$m = \frac{V_G - R_f \cdot I_f}{Z_L \cdot I_G}$$

$$= \frac{1}{Z_L} \left[ \frac{V_G}{I_G} - R_f \cdot \frac{I_f}{I_G} \right]$$

$\frac{I_f}{I_G}$	$R_f$
$\angle = 0$	R only
$\angle > 0$	R and L
$\angle < 0$	R and C

- $I_G$ : Line Current during fault
- $I_f$ : Fault current through the fault resistor  $R_f$ .

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## Derivation of $I_f/I_G$

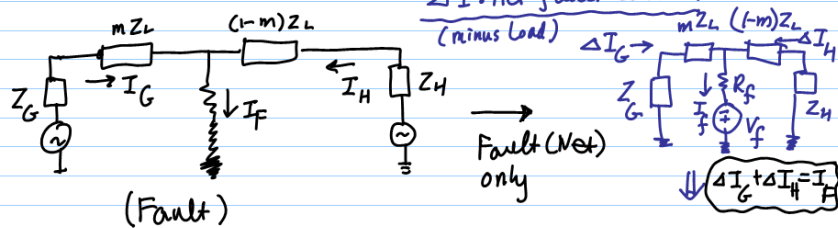
$$\Delta I_G = I_G - I_L$$

Net fault line Component

Note Title

(Superposition: subtract the normal component)

5/9/2010



$$\begin{aligned} \Delta I_G (Z_G + mZ_L) + R_f I_f &= V_f \\ \Delta I_H (Z_H + (1-m)Z_L) + I_f R_f &= V_f \end{aligned} \Rightarrow \begin{aligned} \Delta I_G (Z_G + mZ_L) &= \Delta I_H (Z_H + (1-m)Z_L) \\ \Delta I_H &= \frac{Z_G + mZ_L}{Z_H + (1-m)Z_L} \cdot \Delta I_G \end{aligned}$$

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## Derivation Continued

$$\frac{\Delta I_G}{I_f} \rightarrow \frac{\Delta I_G}{I_f} = d_s$$

$$\frac{I_G}{I_G - I_L} = \frac{I_G}{\Delta I_L} = n_s$$

$$d_s = |d_s| \angle \beta$$

$$n_s = |n_s| \angle \gamma$$

$$I_f = \Delta I_G + \Delta I_H = \Delta I_G \left( 1 + \frac{Z_G + mZ_L}{Z_H + (1-m)Z_L} \right) = \Delta I_G \cdot \frac{Z_G + Z_H + Z_L}{Z_H + (1-m)Z_L}$$

$$\Rightarrow \frac{\Delta I_G}{I_f} = \frac{Z_H + (1-m)Z_L}{Z_G + Z_H + Z_L} = d_s \quad \text{Current Distribution factor}$$

$$\frac{I_G}{\Delta I_G} = n_s \quad \text{Circuit Loading factor}$$

$$Z_{F_G} = \frac{V_G}{I_G} = m \cdot Z_L + R_f \cdot \frac{1}{d_s \cdot n_s}$$

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## Reactive component of fault resistance

- 2 factors

- Current distribution factor,  $d_s$

- Determined by system impedances
    - Angle of  $d_s$  ( $\beta$ ) = 0 if system is homogeneous (Same R/X ratio of lines)

$$\frac{Z_H + (1-m)Z_L}{Z_G + Z_H + Z_L} = d_s$$

- Circuit loading factor,  $n_s$

- Determined by the load current ( $I_L$ ) presence in the system
    - The angle of  $n_s$  ( $\gamma$ ) is not zero if there is a load flow in the system
    - If  $I_G$  is much bigger than  $I_L$ , the angle will approach zero.

$$\frac{I_G}{I_G - I_L} = \frac{I_G}{\Delta I_L} \doteq n_s$$

- Sum of the angles ( $\beta + \gamma$ ) determines the reactive component caused by fault resistance,  $R_f$ .

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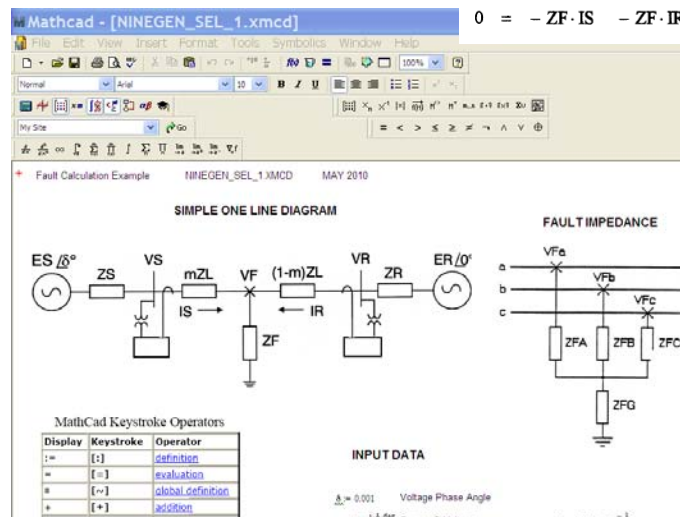
## Practice with MathCad

NINEGEN\_SEL\_1.xmcd  
Mathcad Document  
1,609 KB

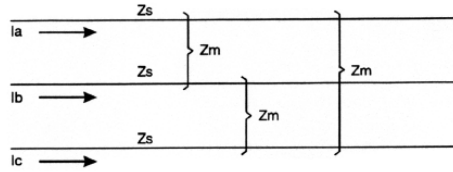
$$ES = ZSS \cdot IS + 0 + VF$$

$$ER = + 0 + ZRR \cdot IR + VF$$

$$0 = - ZF \cdot IS - ZF \cdot IR + VF$$



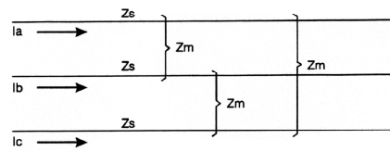
## Mutual Impedance vs. Sequence Impedance



- voltage drop across the A-phase conductor is:  $V_a = Z_s \cdot I_a + Z_m \cdot (I_b + I_c)$
- for the special condition of the balanced current due to a three-phase fault where  $(I_b + I_c) = -I_a$ :  $V_a = (Z_s - Z_m) \cdot I_a$   
Since  $V_a$  and  $I_a$  are positive-sequence quantities, the positive-sequence impedance is:  $z_1 = Z_s - Z_m$  ①
- for another special condition where the currents are equal and in phase  $(I_b + I_c) = 2 I_a$ :  $V_a = (Z_s + 2 \cdot Z_m) \cdot I_a$   
In this case,  $V_a$  and  $I_a$  are zero-sequence quantities; the zero-sequence impedance is:  $z_0 = Z_s + 2 \cdot Z_m$  ②
- From ① and ②, self- and mutual-impedance as functions of  $z_0$  and  $z_1$  for use in the impedance matrix
  - self-impedance:  $z_s(z_0, z_1) = \frac{z_0 + 2 \cdot z_1}{3}$
  - mutual impedance:  $z_m(z_0, z_1) = \frac{z_0 - z_1}{3}$

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## "k factor" from mutual impedance



■ self-impedance:  $z_s = \frac{z_0 + 2 \cdot z_1}{3}$

■ mutual impedance:  $z_m = \frac{z_0 - z_1}{3}$

■ voltage drop across the A-phase conductor is:  $V_a = Z_s \cdot I_a + Z_m \cdot (I_b + I_c)$

$$I_r = I_a + I_b + I_c \rightarrow I_b + I_c = I_r - I_a$$

$$V_a = Z_s \cdot I_a + Z_m \cdot (I_r - I_a) = (Z_s - Z_m) I_a + Z_m \cdot I_r$$

$$= \left( \frac{z_0 + 2 \cdot z_1}{3} - \frac{z_0 - z_1}{3} \right) I_a + \frac{z_0 - z_1}{3} I_r$$

$$= z_1 \cdot I_a + \frac{z_0 - z_1}{3} I_r = z_1 \left( I_a + \frac{z_0 - z_1}{3 z_1} I_r \right) = z_1 (I_a + k_0 \cdot I_r)$$

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## Practical Approaches: (1) Simplification & (2) Limiting errors

- **Various techniques to accommodate the two factors or to reduce the factors**
  - Fault location without using source impedance (Takagi et al)
  - Fault location using source impedance: US Patent 5839093 "System for locating faults and estimating fault resistance in distribution networks with tapped loads" Novosel et al. 1998, ABB
- **Simplification**
  - Reactance Method
  - Voltage Sag
  - Rms V and I

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## Reactance Method

- Measures the apparent impedance
- Determines the ratio of the measured reactance and to the reactance of the entire line, which is proportional to the distance to the fault.
- Assumptions:
  - The current through the fault resistance is in phase with the current at the measurement point
  - There is no load prior to the fault
- One of the earliest algorithms that compensate for the fault resistance by measuring only the imaginary part of the apparent line impedance

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## Reactance Method

- $m$ : per-unit distance to the fault

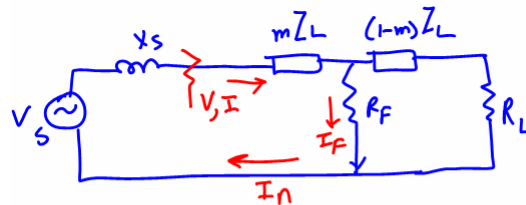
$$\text{From } Z_G = \frac{V_G}{I_G} = m \cdot Z_L + R_f \cdot \frac{I_f}{I_G}$$

$$I_m \left( \frac{V_G}{I_G} \right) = m \cdot I_m(Z_L) + R_f \cdot \underbrace{I_m \left( \frac{I_f}{I_G} \right)}_{=0 \text{ by Assumption}}$$

$$\Rightarrow m = \frac{I_m(V_G/I_G)}{I_m(Z_L)}$$

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## Reactance Method for Ground Fault Case



$$V_a = m \cdot Z_L \cdot (I_a + k I_f) + I_f R_F$$

$$\frac{V_a}{I_f} = \frac{m \cdot Z_L (I_a + k I_f)}{I_f} + R_F$$

$$R_F = \frac{V_a}{I_f} - \frac{m \cdot Z_L (I_a + k I_f)}{I_f}$$

$I_m = 0$

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## Further Approximation

Approximation:

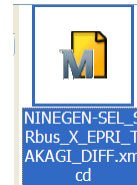
$$V_a = m \cdot Z_L \cdot (I_a + k I_r) + I_F R_F$$

$$\angle I_F = \angle I_r$$

$$V_a \cdot I_r^* = m \cdot Z_L \cdot (I_a + k I_r) \cdot I_r^* + \underbrace{I_F R_F \cdot I_r^*}_{\text{Real}}$$

$$\text{Im}\{V_a \cdot I_r^*\} = m \cdot \text{Im}\{Z_L \cdot (I_a + k I_r) \cdot I_r^*\}$$

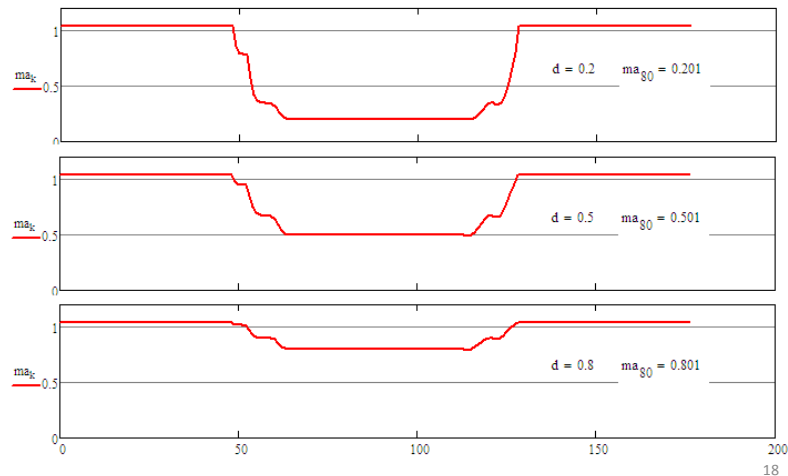
$$m = \frac{\text{Im}\{V_a \cdot I_r^*\}}{\text{Im}\{Z_L \cdot (I_a + k I_r) \cdot I_r^*\}}$$



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## Reactance Approach

$$m = \frac{\text{Im}\{V_a \cdot I_r^*\}}{\text{Im}\{Z \cdot V_a \cdot I_r^*\}}$$



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## Further Approximation

Further Approximation:

$$Z_L \rightarrow jX_L$$

$$I_a + kI_r \rightarrow k' \cdot I_r$$

$$\frac{I_r}{I_p} = \frac{3}{2+K}$$

$$I_a = \frac{2+K}{3} I_r = \frac{2+3k+1}{3} I_r = (k+1)I_r$$

$$I_a + kI_r = (2k+1)I_r = k'I_r$$

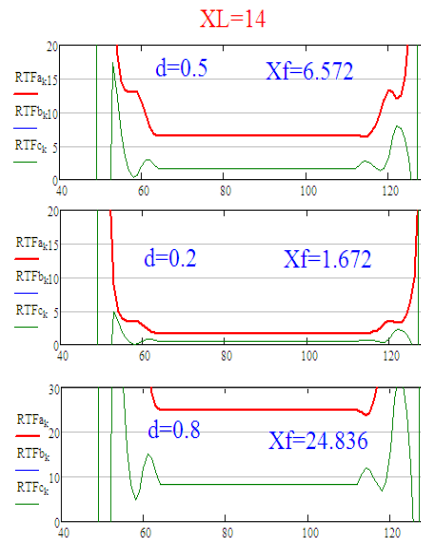
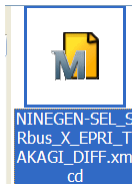
$$m \cdot X_L = \frac{\text{Im} \{ V_a \cdot I_r^* \}}{|I_r|^2} = \frac{|V_a| |I_r|}{k' \cdot |I_r|^2} \sin(\theta_{V_a} - \theta_{I_r})$$

$$X_{TF} = k \cdot \frac{|V_a|}{|I_r|} \sin(\theta_{V_a} - \theta_{I_r})$$

EPRI  
algorithm  
for ground  
fault.

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## Performance



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## Fault Location without Using Source Impedance

### • Improvement

- Elimination of load current by determining the change in current on occurrence of a fault.

From  $V_G = m \cdot Z_L \cdot I_G + R_f \cdot I_f$ ,  $d_s = \frac{\Delta I_G}{I_f}$ ,  $d_s = \frac{Z_H + (1+m)Z_L}{Z_G + Z_L + Z_H}$

$$V_G = m \cdot Z_L \cdot I_G + R_f \cdot \frac{\Delta I_G}{d_s}$$

$\times (\Delta I_G^*)$  both sides, and take only Imaginary parts:

$$I_m(V_G \cdot \Delta I_G^*) = m \cdot I_m[Z_L \cdot I_G \cdot \Delta I_G^*] + R_f \cdot \frac{1}{d_s} \cdot I_m[\Delta I_G^2]$$

Condition: homogenous system  $\rightarrow \angle d_s = 0 \Rightarrow I_m[d_s] = 0$

$$\text{Final Equation: } m = \frac{I_m[V_G \cdot \Delta I_G^*]}{I_m[Z_L \cdot I_G \cdot \Delta I_G^*]}$$

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## Takagi Method - Patent

United States Patent [19]

[11] 4,313,169

Takagi et al.

[45] Jan. 26, 1982

[54] FAULT DETECTING SYSTEM FOR LOCATING A FAULT POINT WITH A FAULT RESISTANCE SEPARATELY MEASURED

[75] Inventors: Toshio Takagi; Yukinari Yamakoshi, both of Tokyo, Japan

[73] Assignee: Tokyo Denryoku Kabushiki Kaisha, Tokyo, Japan

[21] Appl. No.: 63,412

[22] Filed: Aug. 3, 1979

[30] Foreign Application Priority Data

Nov. 13, 1978 [JP] Japan ..... 53-139583

[51] Int. Cl.<sup>3</sup> ..... G01R 31/08; G06F 15/56

[52] U.S. Cl. .... 364/492; 361/80; 324/52

[58] Field of Search ..... 364/492; 324/52; 361/80, 81, 79

[56] References Cited

U.S. PATENT DOCUMENTS

3,710,239 1/1973 Nakamura ..... 324/52  
3,931,502 1/1976 Kojas ..... 324/52 X  
3,983,377 9/1976 Vitins ..... 324/52 X

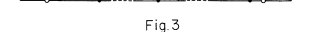
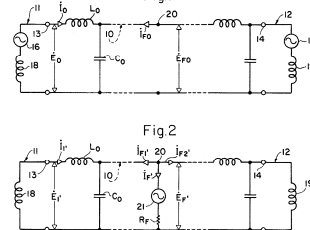
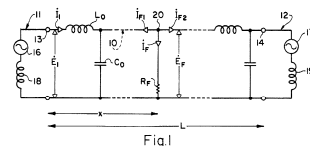
4,063,166 12/1977 Glavitsch et al. .... 324/52  
4,107,778 8/1978 Nii et al. .... 324/52 X  
4,128,805 12/1978 Lanz ..... 324/52  
4,148,087 4/1979 Phadke ..... 324/52 X

Primary Examiner—Edward J. Wise  
Attorney, Agent, or Firm—Frishauf, Holtz, Goodman & Woodward

[57] **ABSTRACT**

At an end (11) of a power detecting system monitors fault in voltage and current the line and calculates the location (20) of the fault by a line constant inherent to the characteristic impedance, to thereby locate the fault by directly using the without affected by the in the fault. The system can be from the distance and those at the end and an opposit

3 Claims, 7 D

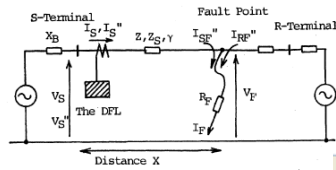


## Takagi Method

$$x = \frac{\text{Im} (V_S \cdot I_F^*)}{\text{Im} (I_S \cdot I_F^*)}$$

where

- $x$ : distance to the fault point
- $V_S$ : voltage of S-terminal
- $I_S$ : current of S-terminal
- $V_F$ : voltage of fault point
- $I_F$ : fault current
- $V_S^0$ : voltage difference between pre-fault and after-fault voltage.
- $I_S^0$ : current difference between pre-fault and after-fault (fault component current)
- $I_{SF}^0$ : fault current from S-terminal
- $Z_S$ : surge impedance
- $Z$ : transmission line impedance per unit length
- $\gamma$ : propagation constant
- $\text{Im}$ : imaginary component
- $*$ : conjugate component



$$R_F = \frac{V_a}{I_F} - \frac{m \cdot Z_L \cdot (I_a + k I_F)}{I_F}$$

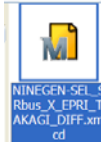
$$I_m = 0$$

Normal

$$I_F = I_a - I_{aV}$$

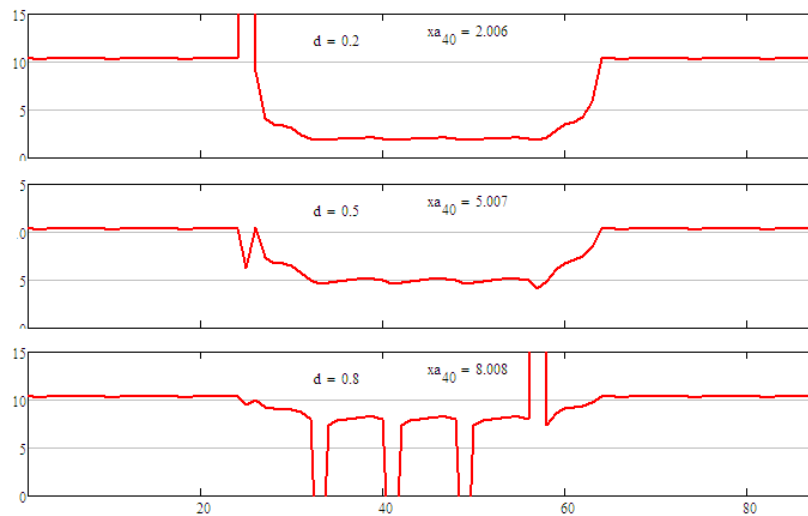
$$Z_L \rightarrow jX_L$$

$$m = \frac{\text{Im} \{ V_a \cdot (I_a - I_{aV})^* \}}{\text{Im} \{ Z_L \cdot I_a \cdot (I_a - I_{aV})^* \}}$$



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## Takagi Approach Example



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## Variation of A2

- Modified method
  - Uses zero-sequence current ( $I_R$ ) ( instead of the net fault current)
  - Uses the angle  $\beta$  of the current distribution factor derived from the source impedance data
  - Accounts for non-homogeneous system
  - Reduces the reactance effect error
  - Problem with accurate correction of  $\beta$ .

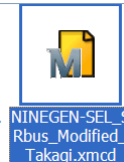
$$m = \frac{I_m (V_c \cdot I_R^* \cdot e^{-j\beta})}{I_m (Z_L \cdot I_G \cdot I_R^* \cdot e^{-j\beta})}$$

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## Further Improvement (Modified Takagi &SEL)

$$V_a = m \cdot Z_{1L} \cdot (I_a + k_0 \cdot I_r) + R_F \cdot I_F$$

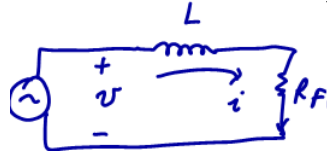
$$\begin{aligned}
 I_F &= |I_F| e^{j\theta_F} \\
 I_r &= |I_r| e^{j\theta_r} \quad I_r^* = |I_r| e^{-j\theta_r} \\
 I_F \cdot I_r^* &= |I_F| |I_r| e^{j(\theta_F - \theta_r)} \\
 I_F \cdot I_r^* \cdot \underbrace{\{e^{j(\theta_F - \theta_r)}\}^*}_A &= |I_F| |I_r| \quad \text{Real} \\
 V_a \cdot A &= m \cdot Z_{1L} \cdot (I_a + k_0 \cdot I_r) \cdot A + R_F \cdot |I_F| |I_r| \\
 I_m \{V_a \cdot A\} &= m \cdot I_m \{Z_{1L} \cdot (I_a + k_0 \cdot I_r) \cdot A\} \\
 \rightarrow m &= \frac{I_m \{V_a \cdot A\}}{I_m \{Z_{1L} \cdot (I_a + k_0 \cdot I_r) \cdot A\}}
 \end{aligned}$$



## Differential Equation Approach

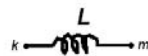
- $L$  calculation from sampled data of  $v$  and  $i$ 
  - Time domain Approach
  - Extraction of  $R$  and  $X$
- Different ways of dealing Derivative ( $d/dt$ ) for *computing from sampled data*
  - Numerical Analysis of Derivative
  - Conversion of the equation into integral, then trapezoidal rule
  - Discretized element model

$$v(t) = R \cdot i(t) + L \frac{di(t)}{dt}$$



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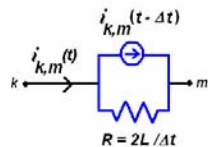
## Discretized Model of Elements – EMTD approach



$$v_k - v_m = L \frac{di_{k,m}}{dt}$$

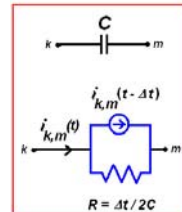
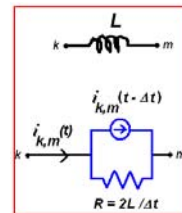
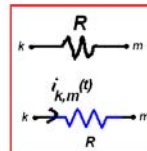
$$i_{k,m}(t) = i_{k,m}(t - \Delta t) + \frac{1}{L} \int_{t-\Delta t}^t (v_k - v_m) dt$$

$$i_{k,m}(t) = I_{k,m}(t - \Delta t) + \frac{\Delta t}{2L} [v_k(t) - v_m(t)]$$



$$I_{k,m}(t - \Delta t) = i_{k,m}(t - \Delta t) - \frac{\Delta t}{2L} [v_k(t - \Delta t) - v_m(t - \Delta t)]$$

Discretization Error:  $(\Delta t)^3$



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## Trapezoidal Approximation

$$v(t) = R \cdot i(t) + L \cdot \frac{di(t)}{dt}$$

$$\int_{t_0}^{t_1} v(t) dt = R \int_{t_0}^{t_1} i(t) dt + L [i(t_1) - i(t_0)]$$

$$\int_{t_1}^{t_2} v(t) dt = R \int_{t_1}^{t_2} i(t) dt + L [i(t_2) - i(t_1)]$$

$$\frac{\Delta t}{2} [v(t_1) + v(t_0)] = R \cdot \frac{\Delta t}{2} [i(t_1) + i(t_0)] + L [i(t_1) - i(t_0)]$$

$$\frac{\Delta t}{2} [v(t_2) + v(t_1)] = R \cdot \frac{\Delta t}{2} [i(t_2) + i(t_1)] + L [i(t_2) - i(t_1)]$$

$$\begin{bmatrix} \frac{\Delta t}{2} [I_{k+1} + I_k] & [I_{k+1} - I_k] \\ \frac{\Delta t}{2} [I_{k+2} + I_{k+1}] & [I_{k+2} - I_{k+1}] \end{bmatrix} \begin{bmatrix} R \\ L \end{bmatrix} = \begin{bmatrix} \frac{\Delta t}{2} [V_{k+1} + V_k] \\ \frac{\Delta t}{2} [V_{k+2} + V_{k+1}] \end{bmatrix}$$

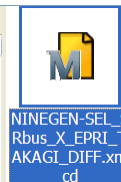
- Source: Arum G. Phadke and James S. Thorp, "Computer relaying for power systems", RSP.Ltd August 1994, pp.118-131

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## Final Form and Practice with MathCad

$$R = \frac{(V_{k+1} + V_k) \cdot (I_{k+2} - I_{k+1}) - (V_{k+2} + V_{k+1}) \cdot (I_{k+1} - I_k)}{(I_{k+1} + I_k) \cdot (I_{k+2} - I_{k+1}) - (I_{k+2} + I_{k+1}) \cdot (I_{k+1} - I_k)}$$

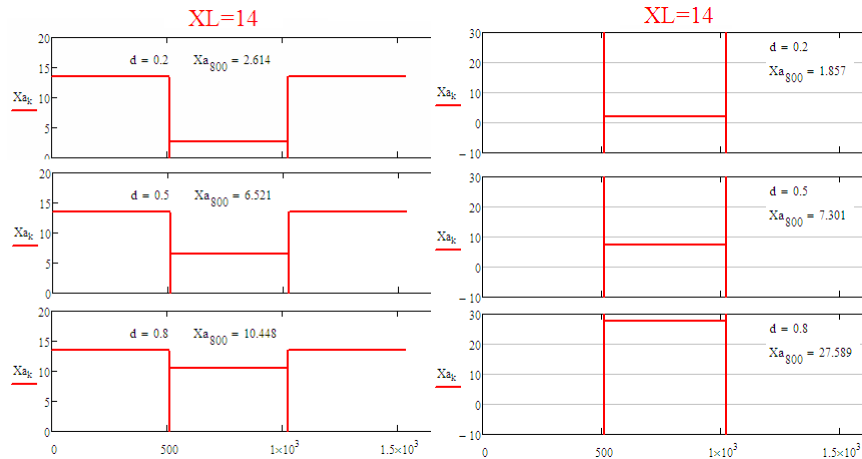
$$X = \left( \int \pi \Delta t \right) \cdot \frac{(I_{k+1} + I_k) (V_{k+2} + V_{k+1}) - (I_{k+2} + I_{k+1}) (V_{k+1} + V_k)}{(I_{k+1} + I_k) (I_{k+2} - I_{k+1}) - (I_{k+2} + I_{k+1}) (I_{k+1} - I_k)}$$



## Differential Equation Approach on SEL

$$v(t) = R \cdot i(t) + L \frac{di(t)}{dt}$$

$$i(t) \begin{cases} i_a(t) + k \cdot I_r \\ k' \cdot I_r \end{cases}$$

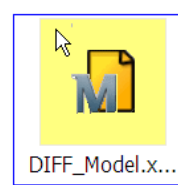
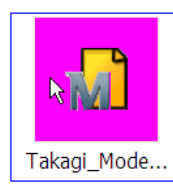
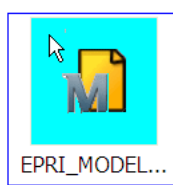
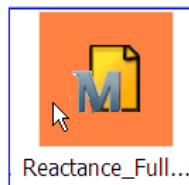


## Fault Location with Actual Data

\* Data Given/tested by Dan Sabin \*\*

\* Last two columns DE (distance by SABIN) and LL (Line length in X) \*

SubstationBus	MMDDYY-HHMMFT	FT	True Distance (X)	Calculated Dist (X)	Line Length (in X)	Line
CreelmanS	102205-031724	CG	2.2	2.83	5.13	CR973
CreelmanS	102205-031731	CG	2.2	2.26	5.13	CR973
CreelmanS	121005-031342	AG	2.09	1.97	5.13	CR973
CreelmanS	121005-031348	AG	2.09	2.1	5.13	CR973
CreelmanS	121005-031433	AG	2.09	2.09	5.13	CR973
CreelmanN	012606-114830	AG	4.2	4.4	10.4	CR237
CreelmanN	022706-222122	BG	1	1.27	10.4	CR237
CreelmanN	121706-225239	BG	4.4	3.79	8	CR972
CreelmanN	121706-225244	BG	4.4	3.86	8	CR972





# Fault location using Source Impedance

**United States Patent** [19] **Patent Number:** 5,839,093  
**Novosel et al.** [45] **Date of Patent:** Nov. 17, 1998

[54] **SYSTEM FOR LOCATING FAULTS AND ESTIMATING FAULT RESISTANCE IN DISTRIBUTION NETWORKS WITH TAPPED LOADS**  
 [75] Inventors: **Damir Novosel, Cary; David Hart, Raleigh; Yi Hu, Cary, all of N.C.; Jorma Myllymaki, Tampere, Finland**  
 [73] Assignee: **ABB Transmit Oy, Vaasa, Finland**  
 [21] Appl. No.: **777,623**  
 [22] Filed: **Dec. 31, 1996**  
 [51] **Int. Cl.** **H02H 3/26**  
 [52] **U.S. Cl.** **702/59; 702/58; 364/528.27; 364/528.28; 364/528.29; 361/65; 361/63; 361/79; 361/80; 324/525**  
 [58] **Field of Search** **364/492, 480-483, 364/550, 551.01, 555, 579, 580, 802, 528.27-528.29, 807, 873, 838; 374/512, 522, 521, 525**

4,499,417 2/1985 Wright et al. 324/533  
 4,559,491 12/1985 Saha 324/522  
 4,841,405 6/1989 Udren 361/80  
 4,857,854 8/1989 Matsushima 324/512  
 4,906,937 3/1990 Wikström et al. 324/523  
 4,996,624 2/1991 Schweitzer et al. 361/63  
 5,072,403 12/1991 Johns  
 5,428,549 6/1995 Chen  
 5,455,776 10/1995 Novosel  
 5,661,664 8/1997 Novosel

**Primary Examiner—Emanuel**  
**Assistant Examiner—Hal D.**

**ABSTRACT**  
 Both fault location and fault resistance are calculated by the present method system takes into account the load flow, thereby calculating consideration the current flow network as well as the effect method calculates fault location.

- The current distribution factor,  $d_s$ , is a function of the source impedance, line impedance, and the unknown fault location.
- If the source impedance is known, fault location can be estimated without the assumption related with the distribution factor.

$$d_s = \frac{Z_L}{Z_s + Z_L} + 1 \quad (2f)$$

$$d_s = \frac{Z_L}{Z_s + Z_L} \left( \frac{Z_s + Z_L}{Z_s} + 1 \right) \quad (2g)$$

$$d_s = \frac{Z_L}{Z_s + Z_L} \left( \frac{Z_s + Z_L}{Z_s} + 1 \right) \quad (2h)$$

The impedances  $Z_s$  AND  $Z_{load}$  are calculated by using Equations 9 and 7 respectively. Complex Equation 22 has two unknowns,  $m$  and  $R_f$ . This equation can be separated into real and imaginary parts. By eliminating  $R_f$ ,  $m$  is given by:

$$m = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad (2i)$$

where:

$$a = 1$$

$$b = \left( \frac{Re(Z_s) \times Re(Z_L)}{Im(Z_s)} \right)$$

$$c = Re(Z_s) \times \frac{Im(Z_s) \times Re(Z_L)}{Im(Z_s)}$$

The inventors have ascertained that the proper solution for  $m$  is given by:

$$m = \frac{-b + \sqrt{b^2 - 4ac}}{2a} \quad (2j)$$

Once an accurate value for  $m$  is obtained, the fault resistance  $R_f$  may be accurately obtained by solving for the imaginary part of equation (22) as follows:

$$R_f = \frac{Im(Z_s)}{Im(Z_s)} - \frac{Im(Z_L)}{Im(Z_s)} \quad (2k)$$

## Quadratic Equation Derivation

From  $d_s = \frac{\Delta I_G}{I_f} = \frac{Z_H + (1-m)Z_L}{Z_s + Z_H + Z_L}$  ( $Z_H \rightarrow Z_{load}$ )

$V_G = m Z_L \cdot I_G + R_f \cdot \frac{\Delta I_G}{d_s}$

$= m Z_L I_G + R_f \cdot \Delta I_G \cdot \frac{Z_s + Z_H + Z_L}{Z_H + (1-m)Z_L}$

$V_G (Z_H + Z_L - m \cdot Z_L) = m (Z_H + Z_L - m \cdot Z_L) \cdot Z_L \cdot I_G$

$+ R_f \cdot \Delta I_G \cdot (Z_s + Z_H + Z_L)$

$I_G \cdot Z_L^2 \cdot m^2 - [(Z_H + Z_L) \cdot Z_L \cdot I_G + V_G \cdot Z_L] m + V_G (Z_H + Z_L)$

$- R_f \cdot \Delta I_G (Z_s + Z_H + Z_L) = 0$

## Continued

$$m^2 - k_1 m + k_2 - k_3 R_f = 0$$

$$\text{where, } k_1 = \frac{V_G}{I_G \cdot Z_L} + \frac{Z_H}{Z_L} + 1$$

$$k_2 = \frac{V_G}{I_G \cdot Z_L} \cdot \left[ \frac{Z_H}{Z_L} + 1 \right],$$

$$k_3 = \frac{\Delta I_G}{I_G \cdot Z_L} \left[ \frac{Z_S + Z_H}{Z_L} + 1 \right]$$

$$Z_S = \frac{V_{GS}}{I_{FS}} - Z_L$$

$$Z_H = \frac{V_{HS}}{I_{FS}} - Z_L$$

Unknowns:  $m$  and  $R_f$

①  $R_f \leftarrow$  by Imaginary part only

$$R_f = -m \cdot \frac{\frac{\text{Im}(k_1)}{\text{Im}(k_3)}}{\frac{\text{Im}(k_2)}{\text{Im}(k_3)}} + \frac{\text{Im}(k_2)}{\text{Im}(k_3)}$$

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## Continued-

ASSIGNMENT

MathCad

②  $m$ : quadratic solution

$$m = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$a = 1$$

$$b = - \left[ \text{Re}(k_1) - \frac{\text{Im}(k_1) \cdot \text{Re}(k_3)}{\text{Im}(k_3)} \right]$$

$$c = -\text{Re}(k_2) - \frac{\text{Im}(k_2) \cdot \text{Re}(k_3)}{\text{Im}(k_3)}$$

### • Problem

- Source Impedance in program must be the same as the actual source impedance of a network

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### Factors affecting the accuracy of the fault estimation

- The combined effect of the load current and fault resistance (reactance effect)
- Influence of zero-sequence mutual effect on the components
- Uncertainty about the zero-sequence impedance
  - Difficult to obtain an accurate zero-sequence impedance ( $Z_{oL}$ ) for line
  - The value is affected by soil resistivity, which can be difficult to measure, and may be changeable.
  - A 20% error in the  $Z_{oL}$  can introduce a 15% error in fault calculation
  - The impedance is not uniformly distributed along the line length (100 to 1 variation in earth resistivity produces about 2 to 1 change in  $Z_o$ )

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### Other Factors of Error

- Insufficient accuracy of the line model (untransposed lines are represented as being transposed and charging capacitance is not considered)
- Presence of shunt reactors and capacitors
- Load flow unbalance
- Measurement errors, CT/PT errors
- Low resolution or sampling rate at measurement station

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## Two-Terminal Data Methods

- Advantages
  - More accurate than one-terminal methods
  - Able to minimize or eliminate the effects of fault resistance, loading, and charging current.
  - Positive Sequence components are used instead of zero-sequence, eliminating the adverse effect of zero-sequence components
- Drawback
  - The data from both ends must be collected at one location
- Required Equipment
  - Measuring devices for 3-phase voltages and currents at each end with time stamping.
  - Communication equipment
  - Central computer for collection of data and calculation of fault location

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## Some other Fault Location Methods

**United States Patent** [19] [11] **Patent Number:** **4,559,491**  
**Saha** [45] **Date of Patent:** **Dec. 17, 1985**

[54] **METHOD AND DEVICE FOR LOCATING A FAULT POINT ON A THREE-PHASE POWER TRANSMISSION LINE**  
 [75] Inventor: **Murari M. Saha, Västerås, Sweden**  
 [73] Assignee: **ASEA Aktiebolag, Västerås, Sweden**  
 Godard, Electrical Utility Load Forecasting, Feb. 1956, AIEE, p. 1428.  
 Stevens et al., Frequency Modulated Fault Locator for Power Lines, Dec. 1971, pp. 1760-1768.  
 Humpage et al., Measuring Accuracy of Distance Protection with Particular Reference to Earth-Fault Con-

(12) **United States Patent** (10) **Patent No.:** **US 6,483,435 B2**  
**Saha et al.** (45) **Date of Patent:** **Nov. 19, 2002**

(54) **METHOD AND DEVICE OF FAULT LOCATION FOR DISTRIBUTION NETWORKS** WO WO 99/46609 9/1999  
 (75) Inventors: **Murari Saha, Västerås (SE); Eugeniusz Rosolowski, Warsaw**  
 (73) Assignee: **ABB AB, Västerås (SE)**  
**United States Patent** [19] [11] **4,107,778**  
**Nii et al.** [45] **Aug. 15, 1978**  
 [54] **DIGITAL FAULT-LOCATION CALCULATION SYSTEM** 3,758,763 9/1973 Nohara et al. .... 235/151.31  
 3,885,199 5/1975 Nohara et al. .... 235/151.31 X  
 3,931,502 1/1976 Kohlas .... 235/151.31  
 [75] Inventors: **Yoshiji Nii, Kawaguchi; Takayuki Matsuda, Tokyo; Yoichi Yamazaki; Haruo Nohara, both of Hitachi, all of Japan** 3,983,377 9/1976 Vains .... 235/151.31  
 3,984,737 10/1976 Okamura et al. .... 361/80  
 [73] Assignees: **Hitachi, Ltd.; The Tokyo Electric Power Co., Inc., both of Japan**  
 [21] Appl. No.: **768,841**  
*Primary Examiner*—Edward J. Wise  
*Attorney, Agent, or Firm*—Craig & Antonelli  
**ABSTRACT**  
 Provided is a digital fault-location calculation system which comprises first means for obtaining data includ-

40

## More

(19) **United States**

(12) **Patent Application Publication**

Premerlani et al.

(10) **Pub. No.: US 2008/0150544 A1**

(43) **Pub. Date: Jun. 26, 2008**

**ASSIGNMENT**

(54) **MULTI-ENDED FAULT LOCATION SYSTEM**

(22) **Filed: Dec. 22, 2006**

(76) **Inventors:** William J. Premerlani, Scottin, NY (US); Bogdan Z. Kaszenny, Markham (CA); Mark G. Adamiak, Paoli, PA (US)

**Publication Classification**

(51) **Int. Cl.** *G01R 31/08* (2006.01)

(52) **U.S. Cl.** ..... 324/521; 324/522

Correspondence Address:  
GENERAL ELECTRIC CO.  
GLOBAL PATENT OPERATION  
187 Danbury Road, Suite 204  
Wilton, CT 06897-4122

**United States Patent**

**Yang**

[19]

US 2008/0150544 A1

[11] **Patent Number: 5,773,980**

[45] **Date of Patent: Jun. 30, 1998**

[54] **ONE-TERMINAL FAULT LOCATION SYSTEM THAT CORRECTS FOR FAULT RESISTANCE EFFECTS**

[75] **Inventor:** Lifeng Yang, Coral Springs, Fla.

[73] **Assignee:** ABB Power T&D Company, Inc., Raleigh, N.C.

4,812,995 3/1989 Gingis et al. .... 324/512 X  
4,906,937 3/1990 Wikstrom et al. .... 324/522  
5,428,549 6/1995 Chua ..... 364/483  
5,455,776 10/1995 Novot ..... 364/492  
5,661,664 8/1997 Novot et al. .... 364/492

**OTHER PUBLICATIONS**

Elmore, Walter, "Evolution of Distance Relaying Principles," 48th Annual Conference for Protective Relay Engineers, Texas A&M University, College Station, Texas, Apr. 3-5, 1995.

(19) **United States**

(12) **Patent Application Publication**

Wahlroos et al.

(10) **Pub. No.: US 2008/0297163 A1**

(43) **Pub. Date: Dec. 4, 2008**

(54) **METHOD FOR DETERMINING LOCATION OF PHASE-TO-EARTH FAULT**

(75) **Inventors:** Ari Wahlroos, Vasa (FI); Janne Altonen, Toijala (FI)

Correspondence Address:  
BUCHANAN, INGERSOLL & ROONEY PC  
POST OFFICE BOX 1404  
ALEXANDRIA, VA 22313-1404 (US)

(51) **Int. Cl.** *G01R 31/08*  
(52) **U.S. Cl.** .....  
(57)

A method and apparatus for determining location of phase-to-earth fault in a power distribution system, comprising a fault current and location

(19) **United States**

(12) **Patent Application Publication**

Wahlroos et al.

(10) **Pub. No.: US 2009/0267611 A1**

(43) **Pub. Date: Oct. 29, 2009**

(54) **APPARATUS AND METHOD FOR DETERMINING LOCATION OF PHASE-TO-PHASE FAULT OR THREE-PHASE FAULT**

(75) **Inventors:** Ari Wahlroos, Vasa (FI); Janne Altonen, Toijala (FI)

**Publication Classification**

(51) **Int. Cl.** *G01R 31/08* (2006.01)

(52) **U.S. Cl.** ..... 324/522

**ABSTRACT**

## More

(19) **United States**

(12) **Patent Application Publication**

Tremblay et al.

(10) **Pub. No.: US 2010/0102824 A1**

(43) **Pub. Date: Apr. 29, 2010**

**ASSIGNMENT**

(54) **ELECTRICAL NETWORK FAULT LOCATION BY DISTRIBUTED VOLTAGE MEASUREMENTS**

(76) **Inventors:** Mario Tremblay, Varennes (CA); Ryszard Pater, Saint-Laurent (CA); Franche Zavoda, Montreal (CA); Mario Germain, Saint-Roch-de-Richelieu (CA)

Correspondence Address:  
MUIRHEAD AND SATURNELLI LLC  
200 FRIDBERG PARKWAY, SUITE 1001  
WESTBOROUGH, MA 01581 (US)

(30) **Foreign Application Priority Data**  
Apr. 18, 2007 (CA) ..... 2,585,820

**Publication Classification**

(51) **Int. Cl.** *G01R 31/08* (2006.01)

(52) **U.S. Cl.** ..... 324/522

(57) **ABSTRACT**

A method of locating a fault on an electrical network energized by a source uses a form of triangulation of voltage measurements at least three different locations on the network, with at least one of the locations situated upstream from the fault with respect to the source. Voltage phasors corre-

(19) **United States**

(12) **Patent Application Publication**

Lubkeman et al.

(10) **Pub. No.: US 2003/0085715 A1**

(43) **Pub. Date: May 8, 2003**

(54) **SYSTEM AND METHOD FOR LOCATING A FAULT ON UNGROUNDED AND HIGH-IMPEDANCE GROUNDED POWER SYSTEMS**

(76) **Inventors:** David Lubkeman, Raleigh, NC (US); Michael J. Gorman, Fitchburg, WI (US); David G. Hart, Raleigh, NC (US)

**Publication Classification**

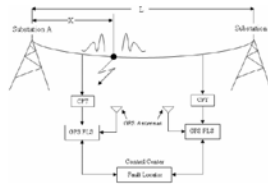
(51) **Int. Cl.** ..... G01R 31/14  
(52) **U.S. Cl.** ..... 324/509

(57) **ABSTRACT**

A fault is located in a power distribution system having a line frequency. The power distribution system includes a plurality of phases, at least one feeder, and each feeder

## Traveling Wave Approach

- Transient Wave Arrival Time
- Transient Wave Frequency Analysis
- Features
  - High sampling of data
  - Transient Frequency correlation to fault distance
  - More suitable for long distance faults



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## Overview of High Frequency/Traveling Wave Methods

- Reflection and transmission of fault generated traveling wave on the faulted point
- Accurate but more complex and expensive in implementation
- Added equipment
  - GPS system
  - Fault transient detectors and diagnosis software
- Difficulties in the configuration and location of fault transient detectors due to complex distribution network

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## Traveling Wave Method

- Correlation of Incident and reflected waveform.
- Single-ended and double-ended approaches
- Big problem in multiple discontinuity (reflection points) in networks
- Variations
  - High frequency signals measured at the substation (with Wavelet analysis) F. H, Magnago and A. Abur (1999) A new fault location technique for radial distribution systems based on high frequency signals. Proc of IEEE PES Summer Meeting, 1:426-431

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## Summated Voltage and Current Wave

- In a total  $n$  lines, with the same value  $Z_0$ , connected to a common bus bar, the summated waves on the line carrying the incident wave is:

$$\text{Summated Voltage Wave} = \frac{Z}{n}$$

$$\text{Summated Current Wave} = 2 - \frac{Z}{n}$$

- As the number of lines connected to a bus bar increases
  - The summated voltage will tend to zero
  - The summated current wave will double
- Observation of current waves (via CT) may be preferable
- But both have been applied.

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## Accuracy Limitation

- Assumption
  - The light speed:  $3 \times 10^8$  m/s
  - Discontinuities in electrical system produces wave reflections
  - Two terminal method allow timing from the initiation of the fault, hence reflected waves are not used.
- Accuracy
  - 300 meters even for long lines
  - Wave detection error due to interpretation of the transient is a major source of error. Many transients and/or reflected transients appear at the same time.
  - One terminal method needs to be more sophisticated – signature analysis required.

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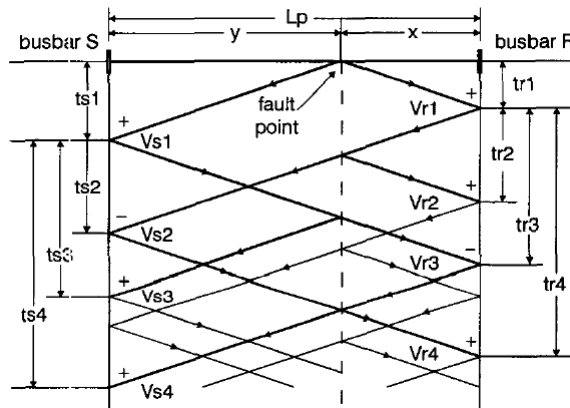
## Traveling Wave Method Modes

- Type A (single-ended) mode
  - Flashover at the fault point launches two waves that travel in opposite directions away from the fault
  - The effective impedances at the line terminals are assumed to be lower than the line surge impedance so that significant reflections are produced which then travel back along the faulty line to the fault point.
  - If the fault arc still exists, and also presents an effective resistance lower than the surge impedance of the line, then any waves arriving at the fault will be almost totally reflected back to the line terminals.
- Type D (two-ended) mode
  - Difference in the times of first arrival of the two fault generated waves at both line terminals are determined.
  - Reflections from other discontinuities, branches, tapped loads, cable sections become unimportant.
- Type E (Single-Ended Circuit Breaker Transient) mode
  - Uses the transients created when a line is re-energized by closing a circuit breaker (close to the Impulse Current Method of fault location widely used on underground cables)

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## Loss Free Overhead Line



The distinction between the reflected wave from the fault point and that from the remote bus bar is vital.

- Detection Device at S

$$x = \frac{v * tr2}{2}$$

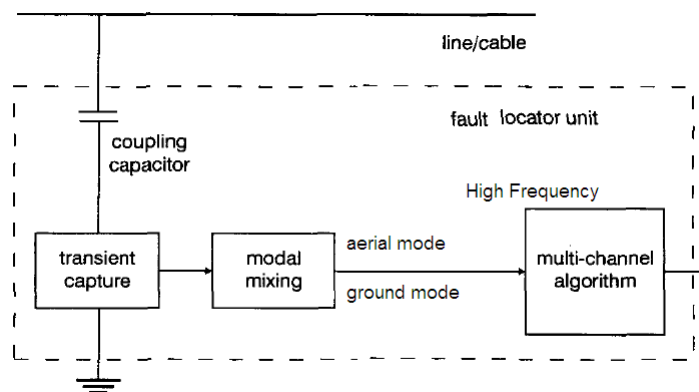
- Detection Device at R

$$x = \frac{v * ts2}{2}$$

$$y = Lp - \frac{v * ts2}{2}$$

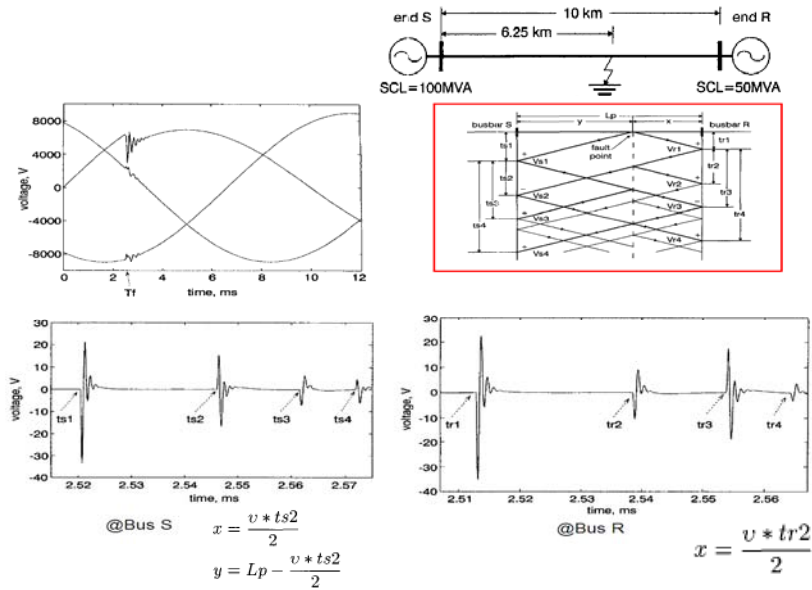
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## Example Fault Locator



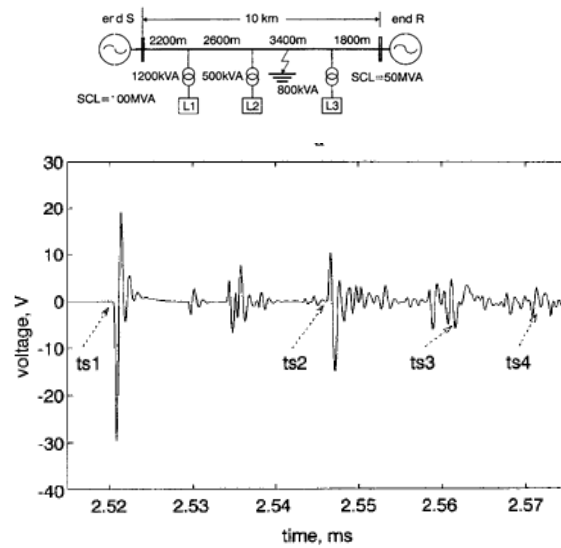
50

## Test 1



1

## Test 2 (with load)



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## Can we apply the algorithms to Distribution Systems Faults?

- Numerous factors affecting the algorithms in distribution networks
  - Conductor size change
  - Multiple feeder taps and laterals
  - Inaccurate models and system data and dynamic configuration
  - Effects of fault impedance
  - Different Grounding Methods
    - Solid grounding
    - Ungrounded Network
    - Peterson's coil
    - Resistance Grounded

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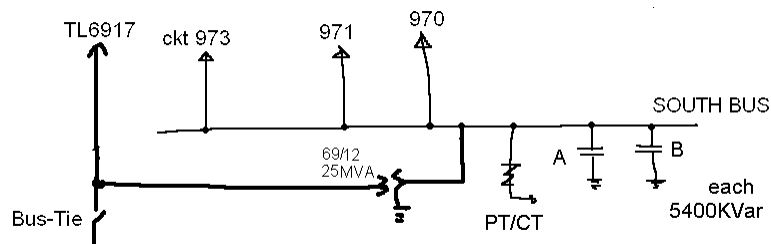
## Distribution Network Topology

- Heterogeneous Feeders
  - Different size and length of cables
  - Presence of overhead and underground lines
  - Presence of single, double, and three-phase loads
  - Presence of laterals along the main feeder
  - Presence of load taps along the main feeder and laterals.
- Cause of estimation error in fault locations
- Model
  - Lumped parameter model
  - Symmetrical components on phasor-based algorithms
- Single line to ground fault is most common
- Different values of fault resistance

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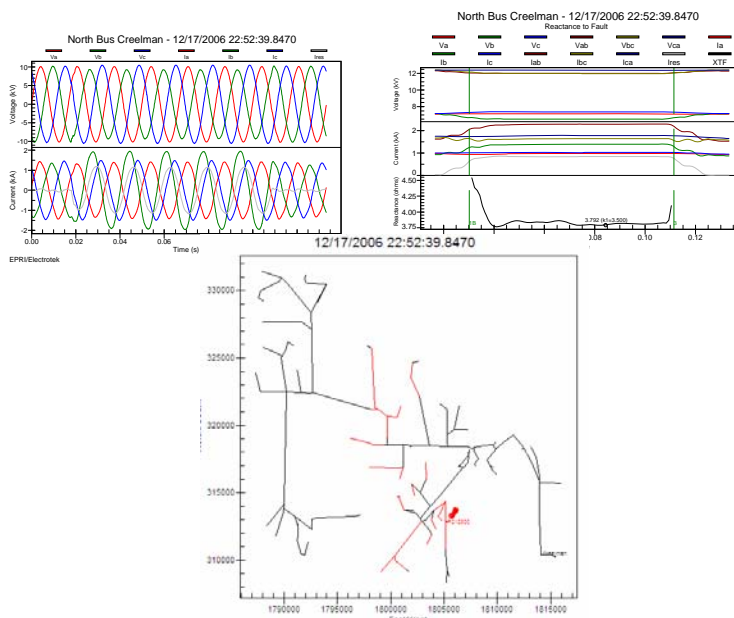
## Fault Location at SDG&E

- Fault Location Efforts
  - Data Measurement (“PQNode”) at 36 Substations
  - Data Analysis using PQView
  - Algorithm (“reactance approach”) Programmed by EPRI
  - Off-line Evaluation for a few Substation Circuits



55

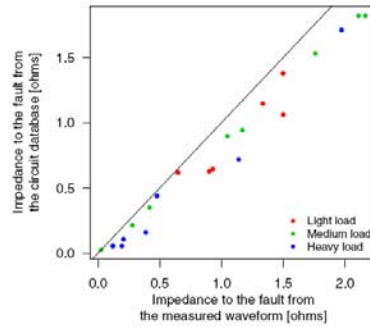
## Fault Location – EPRI Example



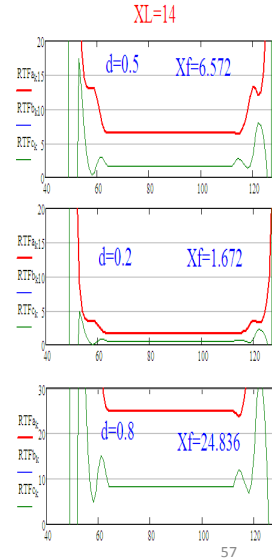
56

## Strength and Weakness of the Current Approach

- Current approach
  - Simple and Effective
  - Load dependency
    - Overreaching & Underreaching Problem

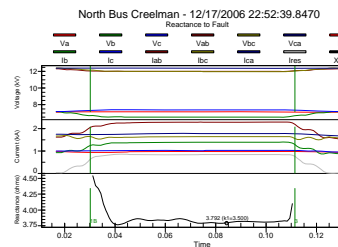
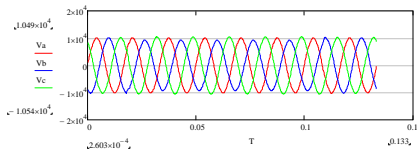
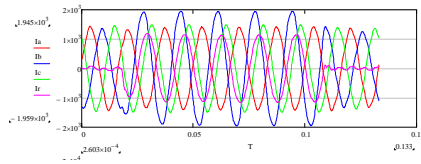


**EPRI** ELECTRIC POWER RESEARCH INSTITUTE  
**Distribution Fault Location**  
 Field Data and Analysis  
 1012438 Final Report, December, 2006  
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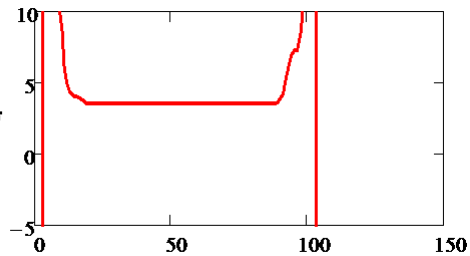


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## Reproduction of EPRI Approach



RTF

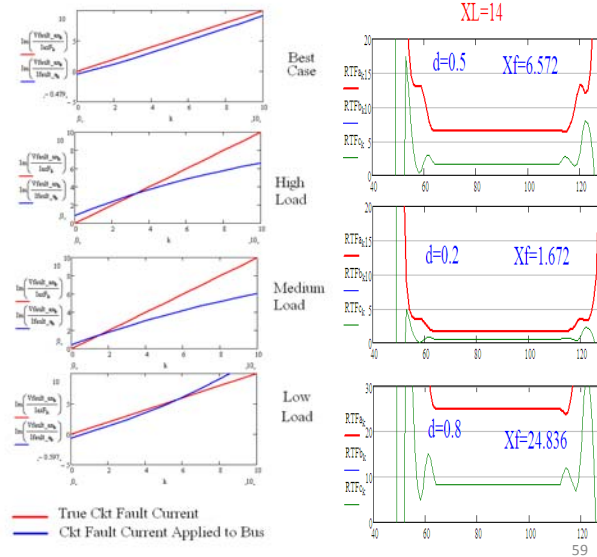


$$X = k \frac{V}{I_r} \sin \theta$$

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## Strength and Weakness of the Current Approach

- Current approach
  - Simple and Effective
  - Load dependency
    - Overreaching & Under-reaching Problem
  - Minimum Data Length Requirement --- at least 2 cycles of faulted data are needed.

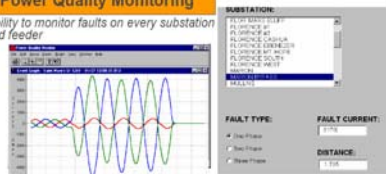


## Simpler Approach

- RMS current Only
  - Fault Current Calculation at each every node
  - Look-up Table

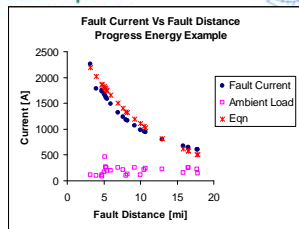
### Power Quality Monitoring

Ability to monitor faults on every substation and feeder



### Interfaces to many different systems required

- Feeder Monitoring System FMS
- DIS mapping
- FMS Fault Locator
- Distribution feeder models (CYME)



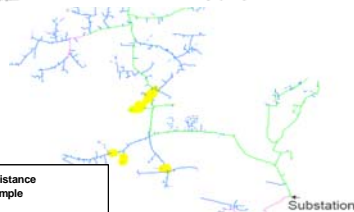
$$d = \frac{-b + \sqrt{b^2 - 4ac}}{2a}$$

$$a = Z_s^2$$

$$b = 2R_s R_{line} + 2X_s X_{line}$$

$$c = Z_{pre}^2 - \left( \frac{V_{pre}}{I_{fault}} \right)^2$$

$R_s$  = source resistance, ohms  
 $X_s$  = source reactance, ohms  
 $Z_s$  = absolute value of the source impedance, ohms  
 $R_{line}$  = line resistance, ohms per unit distance  
 $X_{line}$  = line reactance, ohms per unit distance  
 $Z_{line}$  = absolute value of the line impedance, ohms per unit distance  
 $I_{fault}$  = absolute value of the rms current during the fault, amperes  
 $V_{pre}$  = absolute value of the rms voltage just prior to the fault, volts



## Characterization of Specific Fault

- Voltage-Dip Energy Index ( $E_{\text{dip}}$ )
  - Characterization of specific fault
  - Integration of the drop in signal energy over the duration of an event.
  - $V(t)$ : RMS voltage over time
  - $V_{\text{nom}}$ : Rated voltage

$$E_{\text{dip}} = \int_0^T \left( 1 - \left[ \frac{V(t)}{V_{\text{nom}}} \right]^2 \right) dt$$

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## Fault Location by RMS current – main tool

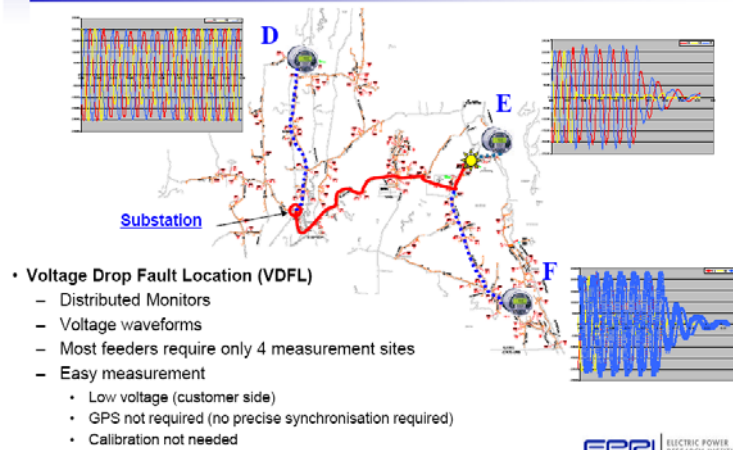
- Determine the average of RMS current during the fault (initial and steady-state portions) duration
- Determine the current index:  $I_{\text{index}}$ 
  - p: predicted value
  - Exp: experimental value
- Compare the current index at several nodes determined by DSFL (by fault current & recloser, etc ?)
- Pick the location where the current index is minimum (i.e., the least error location between model vs actual)

$$\bar{I}_{\text{rms}} = \frac{1}{t_f} \int_0^{t_f} I_{\text{rms}} dt \quad I_{\text{index}} = \sqrt{\left| \frac{1}{2} \sum_k \left[ 1 - \left( \frac{\bar{I}_{\text{rms}}^p}{\bar{I}_{\text{rms}}^{\text{exp}}} \right)^2 \right] \right|}$$

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## Example

### Fault Location based on distributed monitoring (Hydro Quebec example)



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## Other Methods

- **Distributed Devices**
  - Voltage Sensor matrix
  - Voltage magnitude and phase angle table of all sections and nodes in the network
  - Measured data vs. historical fault data.
- **Hybrid Methods**
  - Fault distance calculation & Distributed Device Method
- **Fault Indicator Methods**
- **Use of Smart Meters and Smart Grid Communication Infrastructure**

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## References

- L. Nastac and A. Thatte, “Distribution Systems Fault Locator” Electrical Infrastructure Technology, Training and Assessment Program, DOE Technical Report under Cooperative Agreement DE-FC02-04CH11241, September 30, 2006
- L. Nastac, “Advanced Fault Analysis Software (or AFAS) for Distribution Power Systems,” Center for Grid Modernization Program, DOE Technical Report under Cooperative Agreement DE-FC02-05CH11298, July 31, 2007.
- Numerous US patents and patent publications