

**Note16: 3-phase example problems**

EX#1. A balanced three-phase Y-connected generator has a voltage of 120 V/φ. A balanced 3-phase Δ-load is fed from the source through a distribution line having an impedance of  $0.5 + j 1.4 \Omega/\phi$ . The load impedance is  $118.5 + j 85.8 \Omega/\phi$ . Use the a-phase voltage of the generator as the reference.

- (a) construct 3-phase circuit
- (b) construct a single-phase equivalent circuit
- (c) calculate the line currents  $\mathbf{I}_{aA}$ ,  $\mathbf{I}_{bB}$ ,  $\mathbf{I}_{cC}$ .
- (d) calculate the phase voltages at the load.
- (e) calculate the total complex power delivered to the load
- (f) calculate what percentage of the real power at the sending end of the line is delivered to the load?

**SOLUTION:**

(a)

(b)

(c)  $I_{aA} =$

(d)  $V_{AB} =$

(e)  $S_T =$

(f)  $P_{sending} = P_{load} + P_{loss(line)}$

EX#2. A balanced 3-phase Y-load requires 480kW at a lagging power factor of 0.8. The load is fed from a line having an impedance of  $0.005+j0.025 \Omega/\phi$ . The line voltage at the terminals of the load is 600V.

- (a) construct 3-phase circuit
- (b) construct a single-phase equivalent circuit
- (c) magnitude of the line current
- (d) magnitude of the line voltage at the sending end of the line
- (e) power factor at the sending end of the line

### SOLUTION

(a)

(b)

(c)  $|I_{aA}| = ?$

(i) Method 1:  $S_A =$

(ii) Method 2:  $P_{3\phi} =$

(iii) Method 3:  $P_A =$

(d) From  $V_{an}$

(e) power factor

(i) Method 1:  $pf = \cos(\theta_v - \theta_i)$

(ii) From  $S_{A(\text{sending})} = S_{A(\text{load})} + S_{A(\text{line})}$  (hint: *cosine* of angle of  $S$  is the *pf*)