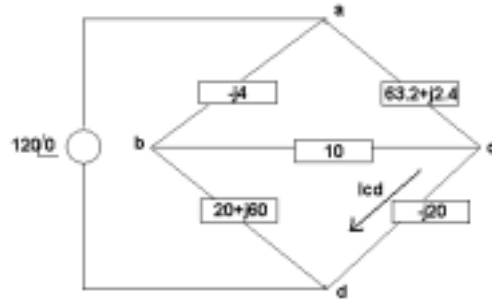


Note 11: Phasor Transformation Application Examples

1. Δ-Y Transformation:

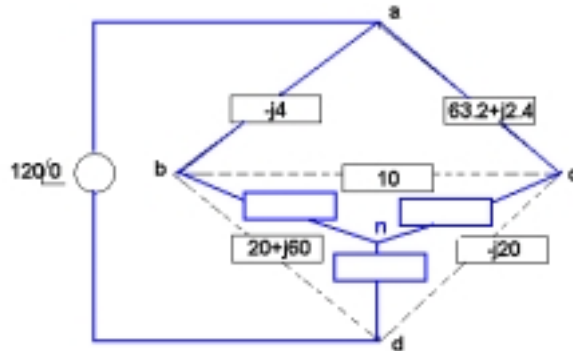
Q: Find current I_{cd} in the circuit below.



Solution:

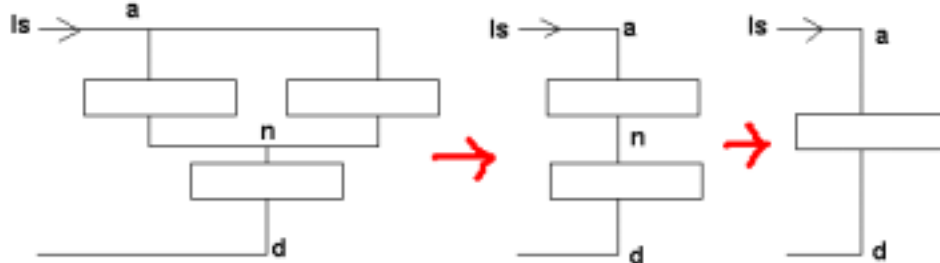
(1) From the circuit above, we see two delta's (top and bottom), and we know that we have to convert one of them to Y-shape. Which delta do you choose to convert to Y-shape? Why?

(2) By your answer above, we decide to convert the bottom one. Then, Y-impedances are as follows, after applying the delta-Y transformation:



(3) Remember, one more node ("n") is added. But, our target is still the current between the nodes "c" and "d". That means: $I_{cd} = \frac{V_{cd}}{-j20}$

The above circuit is simplified to, by impedance summations:



(4) Let's get some analysis here:

Since our target is the voltage between node c and node d, we have to derive a few voltage equations.

First, $V_{cd} = (\text{-----}) + (\text{-----})$

Second, $(\text{-----}) = I_s \cdot (\text{-----})$

Third, $(\text{-----}) =$

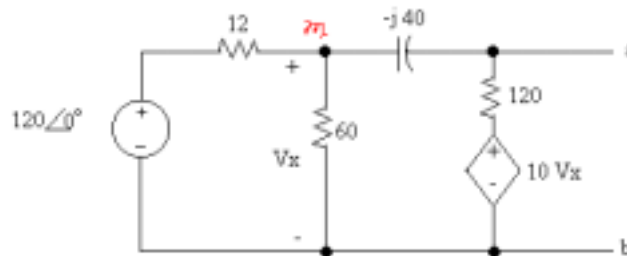
Therefore, $V_{cd} =$

(5) Finally,

$$I_{cd} = \frac{V_{cd}}{-j20} =$$

2. Thevenin Equivalent Circuit Problem:

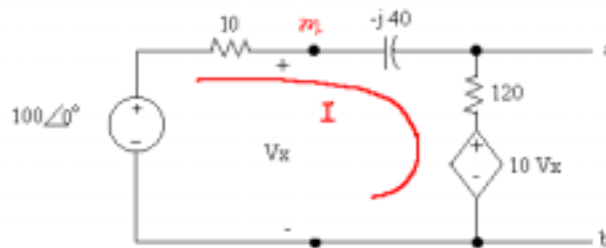
Q.Find the Thevenin equivalent circuit at the terminals *a* and *b* of the circuit below.



SOLUTION

(1) Since there is another node other than *a* and *b*, let's mark it as *m*.

(2) We can simplify the circuit left of the nodes *m* and *b* by applying a few source transformations, as shown below.



(3) Let's find and express the constraint, V_x .

V_x is the voltage from m through a to b . So the V_x equation is: $V_x = \underline{\hspace{2cm}}$

(4) Let's express the Thevenin (or terminal a and b) voltage using the constraint:

$$V_{th} = V_{ab} = \underline{\hspace{2cm}}$$

(5) Now, let's apply KVL around.

KVL equation:

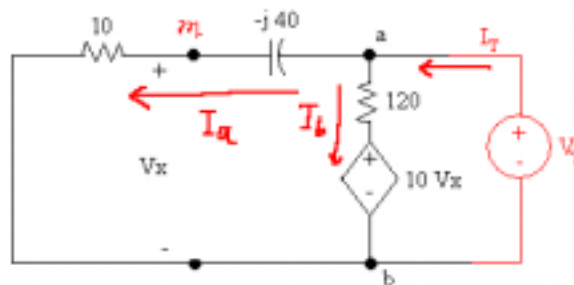
Therefore, the current I : $\bar{I} = \underline{\hspace{2cm}}$

(6) From the equation we got at (4) above, we have the following equation for the Thevenin voltage:

$$V_{th} = V_{ab} = \underline{\hspace{2cm}}$$

Part 2: R_{th}

(1) Let's deactivate the independent source. Also, let's apply a test source. Also, mark two branch currents as I_a and I_b . Then the circuit becomes like this:



(2) Note that the node voltage V_a is same as the test voltage V_T .

Also, the constraint equation around V_x can be expressed by: $V_x = \underline{\hspace{2cm}}$

In addition, the current I_a is: $I_a = \underline{\hspace{2cm}}$

(3) Let's express the test current at node a :

$$I_T = I_a + I_b = \underline{\hspace{2cm}}$$

Arranging the above equation, we have:

$$I_T = \underline{\hspace{2cm}}$$

(4) Therefore,

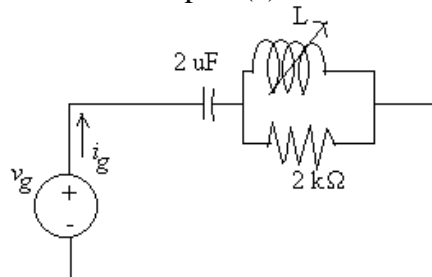
$$Z_{th} = \frac{V_T}{I_T} = \underline{\hspace{2cm}}$$

(5) Finally, the Thevenin equivalent circuit is:

3. Phasor Example: In-phase Condition

Q. The circuit shown below is operating in the sinusoidal steady state. The inductor is adjusted until the current i_g is in-phase with the sinusoidal voltage v_g .

- Specify the inductance (in Henry) if $v_g = 100 \cos 500t$ [V].
- Find i_g when L has the value found in part (a).



SOLUTION:

Part (a):

(1) “In-Phase” relationship means that there is no phase shift between the voltage and the current. This happens only when the overall impedance of the circuit behaves like a pure resistor.

(2) So the strategy here is to apply the “in-phase” condition to the total impedance.

(3) The impedance made by the variable inductor and the 2000 ohm resistor is:

Impedance Expression here:

(4) Therefore the total impedance is: _____
Total Impedance Expression Here:

$$Z = \underline{\hspace{10em}}$$

(5) Since the total impedance should be purely resistive, the imaginary part of the above impedance must be zero.

$$L = \underline{\hspace{10em}}$$

Part(b):

$$I = \underline{\hspace{10em}}$$