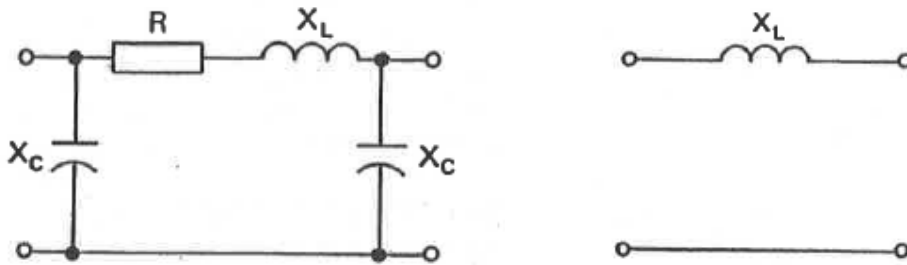


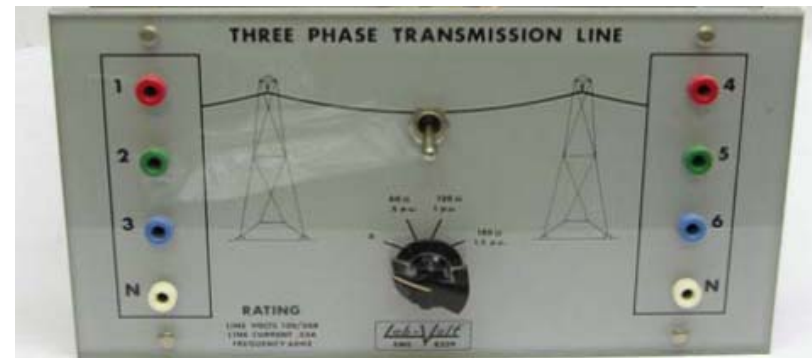
Lab 4- Power Flow and Voltage Regulation

⌘ Transmission Line Representation ("Model")

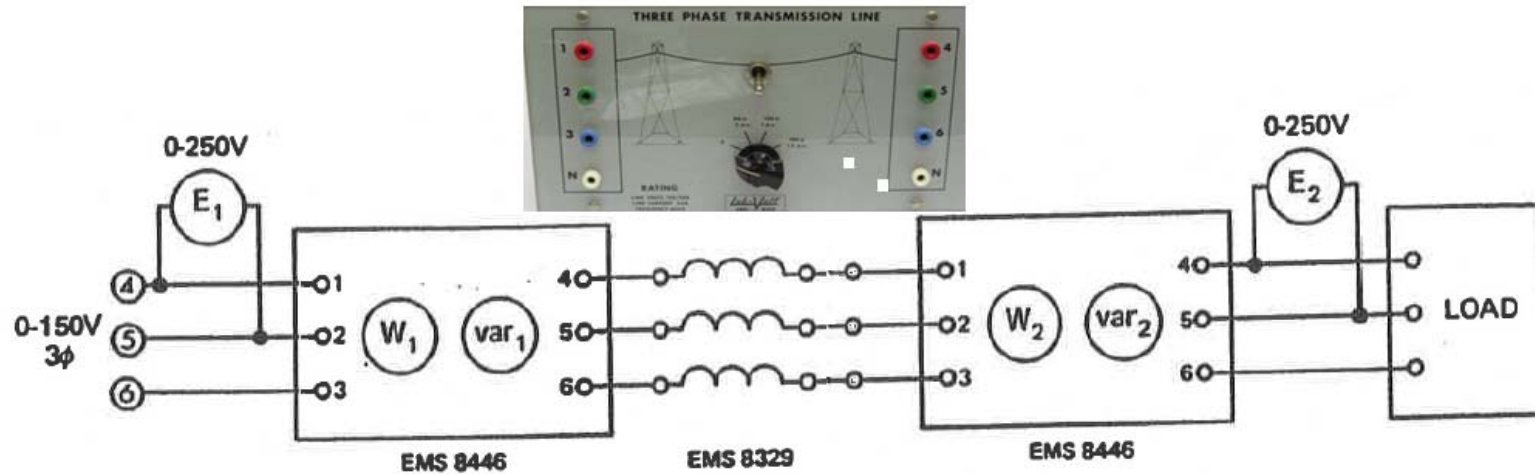


⌘ Voltage Regulation:
Load Voltage Difference Between
V (open, no-load) and V (with Load)

$$\% \text{ regulation} = \frac{(E_0 - E_L) \times 100}{E_0}$$



Transmission Line Loss (Q) + Load (P and Q)

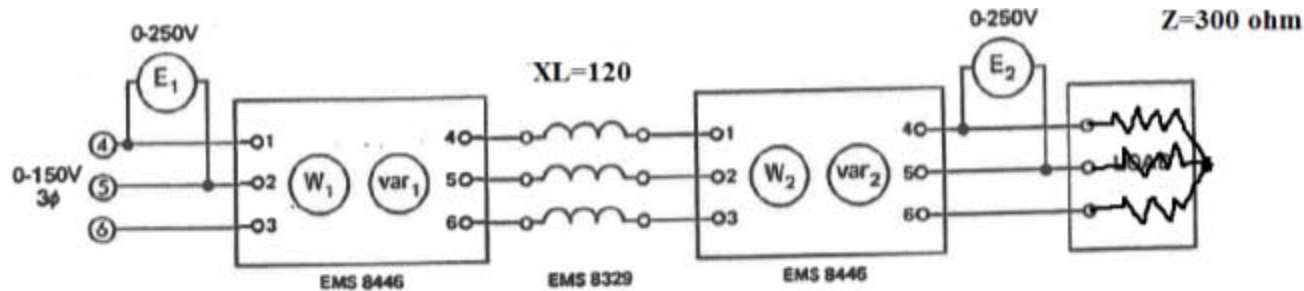


Total P = W₁
Total Q = Var 1

Transmission
P = W₁ - W₂
Q = Var1 - Var 2

Load
P = W₂
Q = Var 2

Example



$$V_L = 150 \quad V_P = \frac{V_L}{\sqrt{3}} = 86.60254 \quad Z_{tr} = 0 + i \cdot 120 \quad Z_{load} = 300 + i \cdot 0 = 300$$

$$Z = Z_{tr} + Z_{load} \quad Z = 300 + 120 \cdot i$$

$$I_L = \frac{V_P}{Z} = 0.248858 - 0.099543 \cdot i$$

$$\theta_v = \arg(V_P) = 0 \quad \theta_i = \arg(I_L) = -0.380506 \quad \theta = \theta_v - \theta_i = 0.380506$$

$$P_{tot} = 3 \cdot |V_P| \cdot |I_L| \cdot \cos(\theta) = 64.655172$$

$$Q_{tot} = 3 \cdot |V_P| \cdot |I_L| \cdot \sin(\theta) = 25.862069$$

$$S_{tr} = 3 \cdot \|I_L\|^2 \cdot Z_{tr} = 25.862069 \cdot i \quad P_{tr} = \text{Re}(S_{tr}) = 0 \quad Q_{tr} = \text{Im}(S_{tr}) = 25.862069$$

$$S_{load} = 3 \cdot \|I_L\|^2 \cdot Z_{load} = 64.655172 \quad P_{load} = \text{Re}(S_{load}) = 64.655172$$

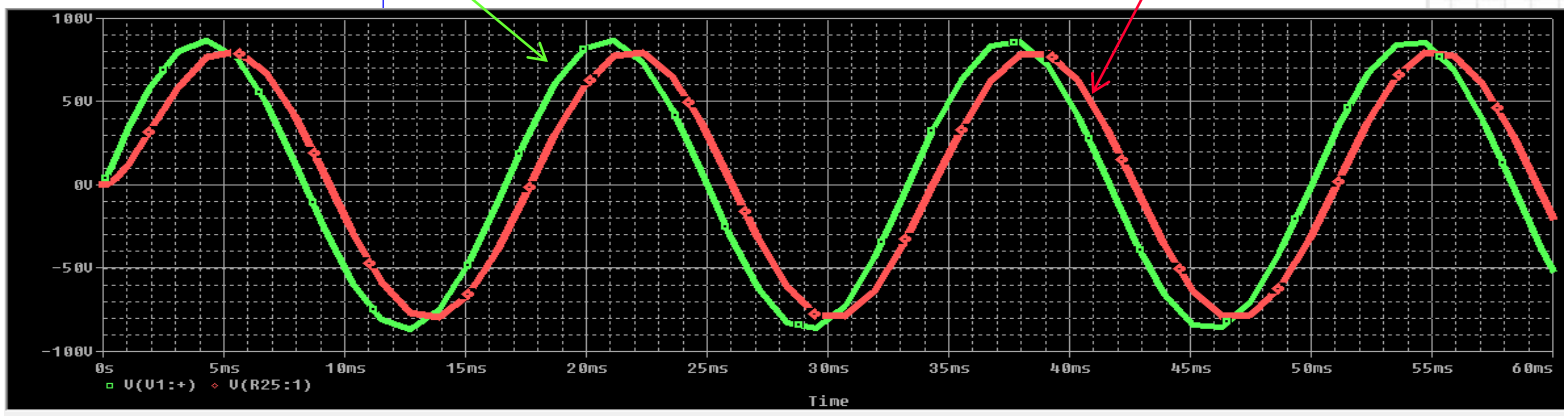
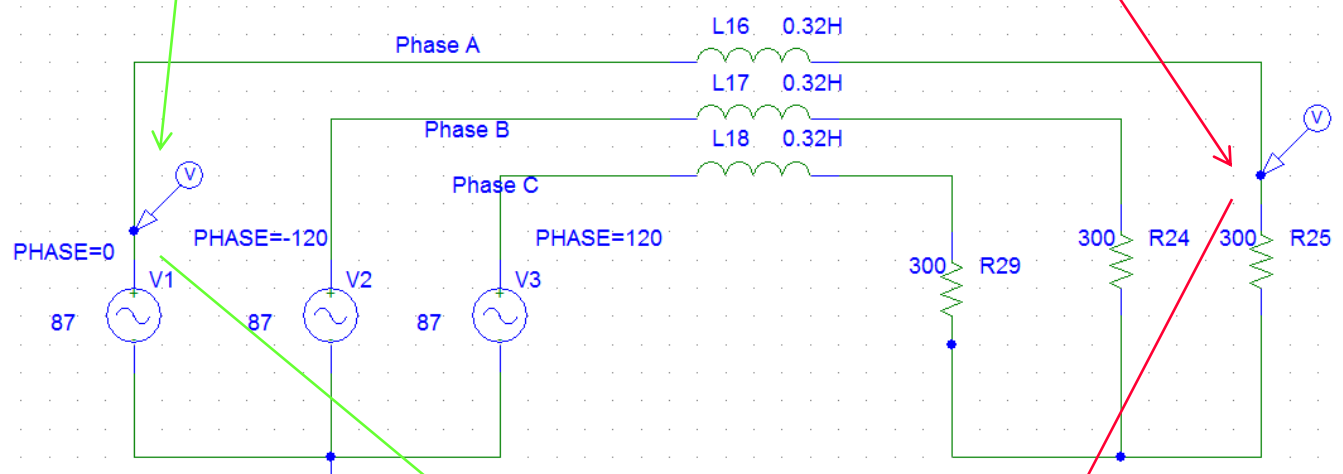
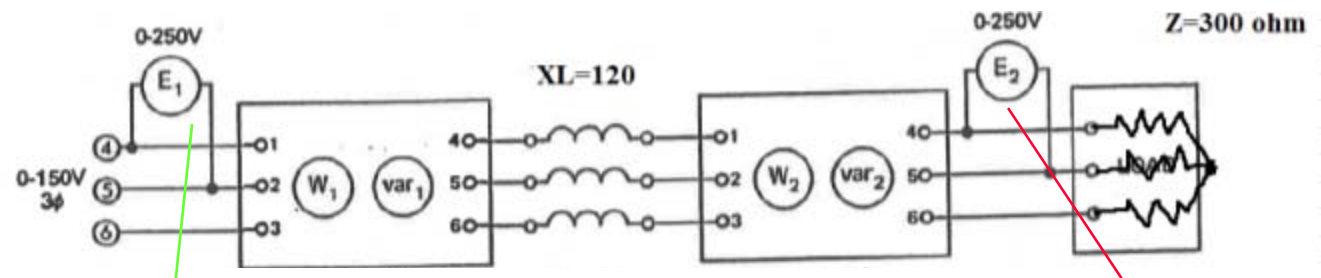
$$\text{Voltage Regulation} \quad Q_{load} = \text{Im}(S_{load}) = 0$$

$$V_{load} = I_L \cdot Z_{load} = 74.657362 - 29.862945 \cdot i$$

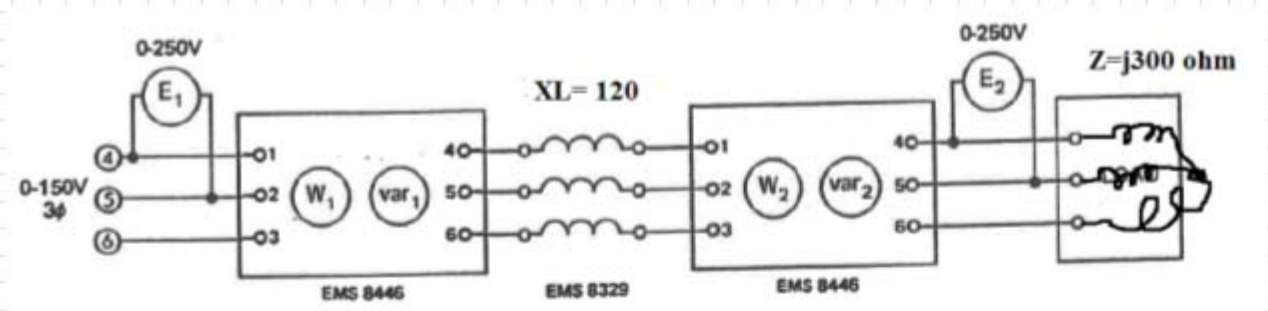
$$|V_{load}| = 80.40844$$

$$\frac{|V_P| - |V_{load}|}{|V_P|} \cdot 100 = 7.152331 \quad \text{percent}$$

Example

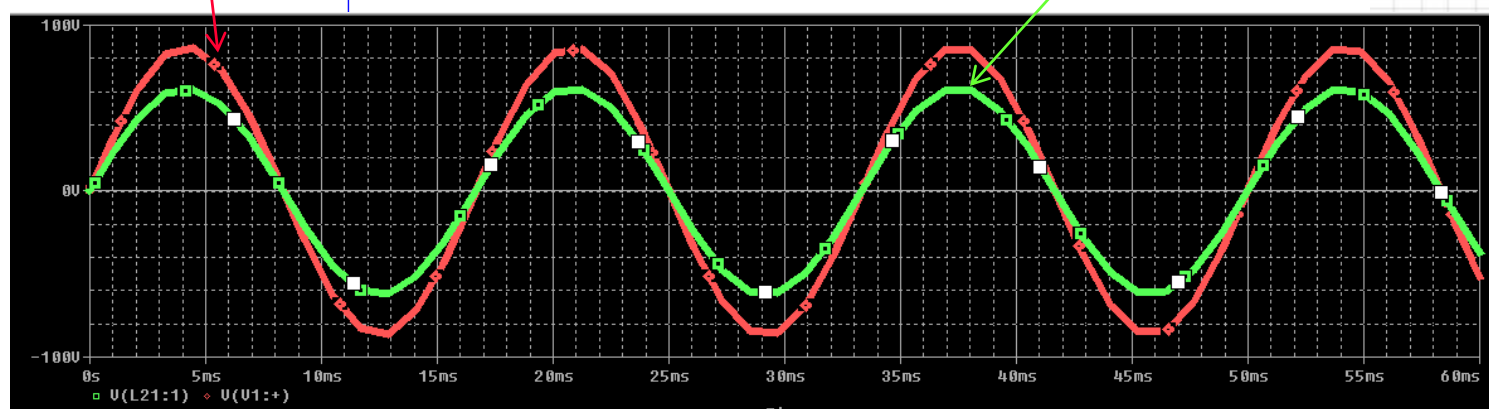
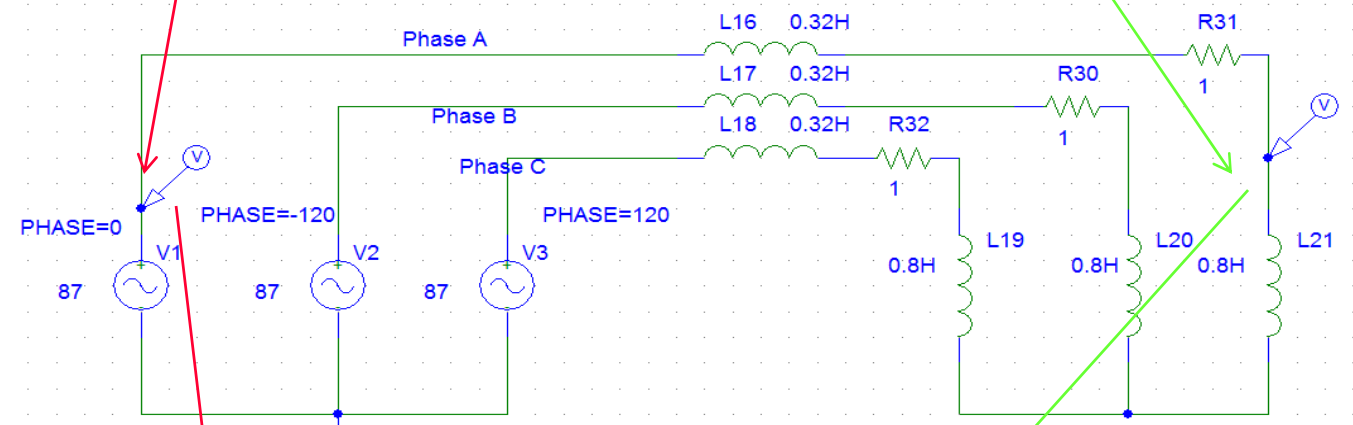
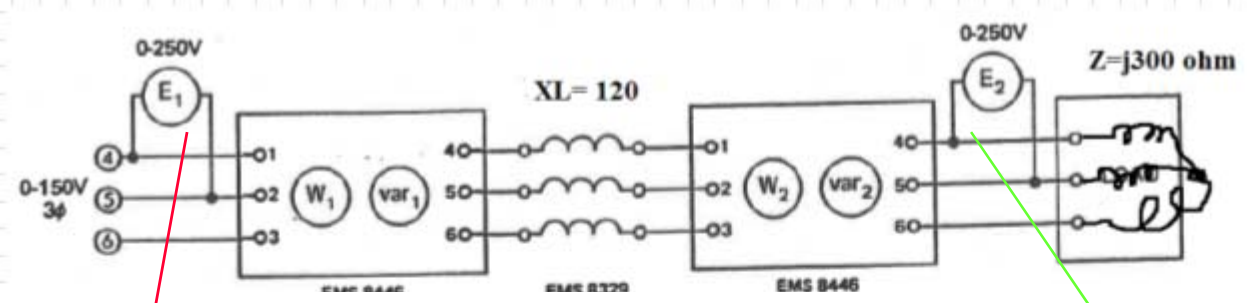


Example C

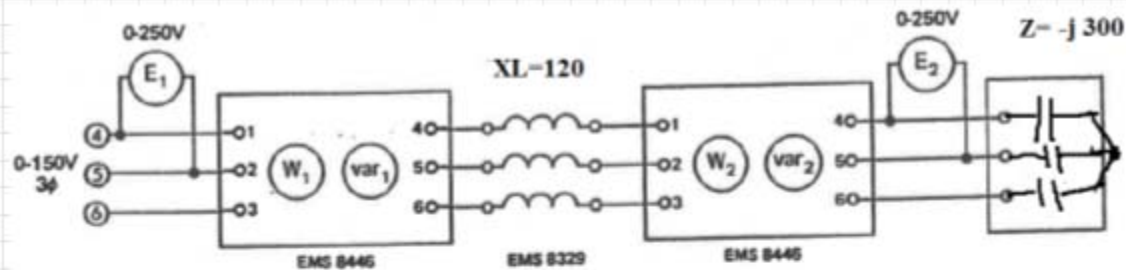


$$\begin{aligned}
 V_L &= 150 & V_P &= \frac{V_L}{\sqrt{3}} = 86.60254 & Z_{tr} &= 0 + i \cdot 120 & Z_{load} &= -i \cdot 300 - 300 \cdot i \\
 Z &= Z_{tr} + Z_{load} & Z &= 420 \cdot i & I_L &= \frac{V_P}{Z} = -0.206197 \cdot i \\
 \theta_v &= \arg(V_P) = 0 & \theta_i &= \arg(I_L) = -1.570796 & \theta &= \theta_v - \theta_i = 1.570796 \\
 P_{tot} &= 3 \cdot |V_P| \cdot |I_L| \cdot \cos(\theta) = 1.870438 \cdot 10^{-13} \\
 Q_{tot} &= 3 \cdot |V_P| \cdot |I_L| \cdot \sin(\theta) = 53.571429 \\
 S_{tr} &= 3 \cdot |I_L|^2 \cdot Z_{tr} = 15.306122 \cdot i & P_{tr} &= \text{Re}(S_{tr}) = 0 & Q_{tr} &= \text{Im}(S_{tr}) = 15.306122 \\
 S_{load} &= 3 \cdot |I_L|^2 \cdot Z_{load} = 38.265306 \cdot i & P_{load} &= \text{Re}(S_{load}) = 0 & Q_{load} &= \text{Im}(S_{load}) = 38.265306 \\
 V_{load} &= I_L \cdot Z_{load} = 61.858957 \\
 \frac{|V_P| - |V_{load}|}{|V_P|} \cdot 100 &= 28.571429 \text{ percent}
 \end{aligned}$$

Example C



Example

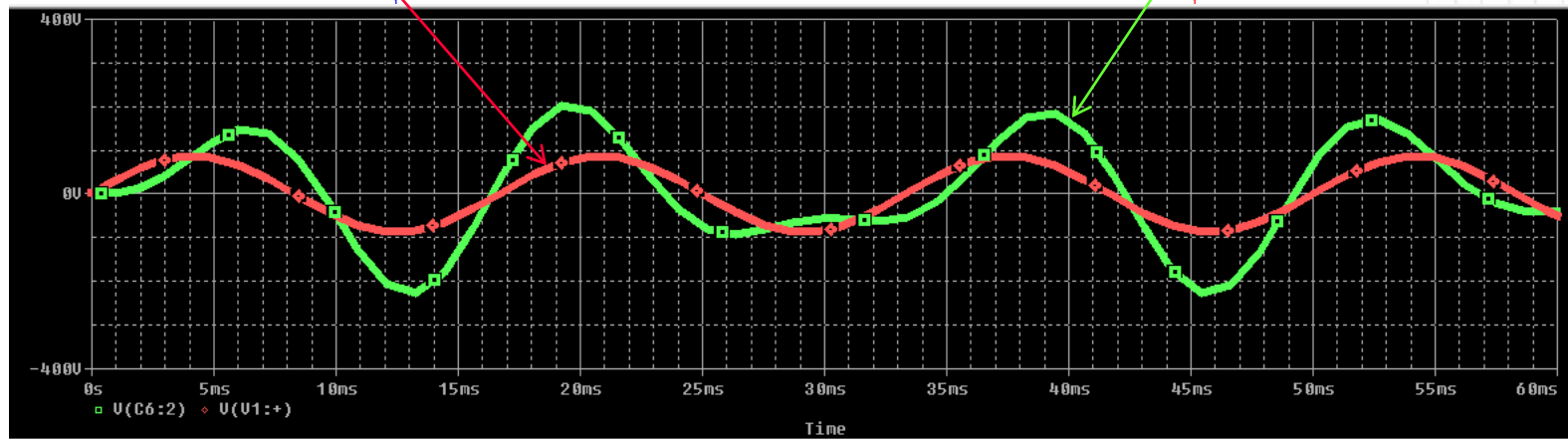
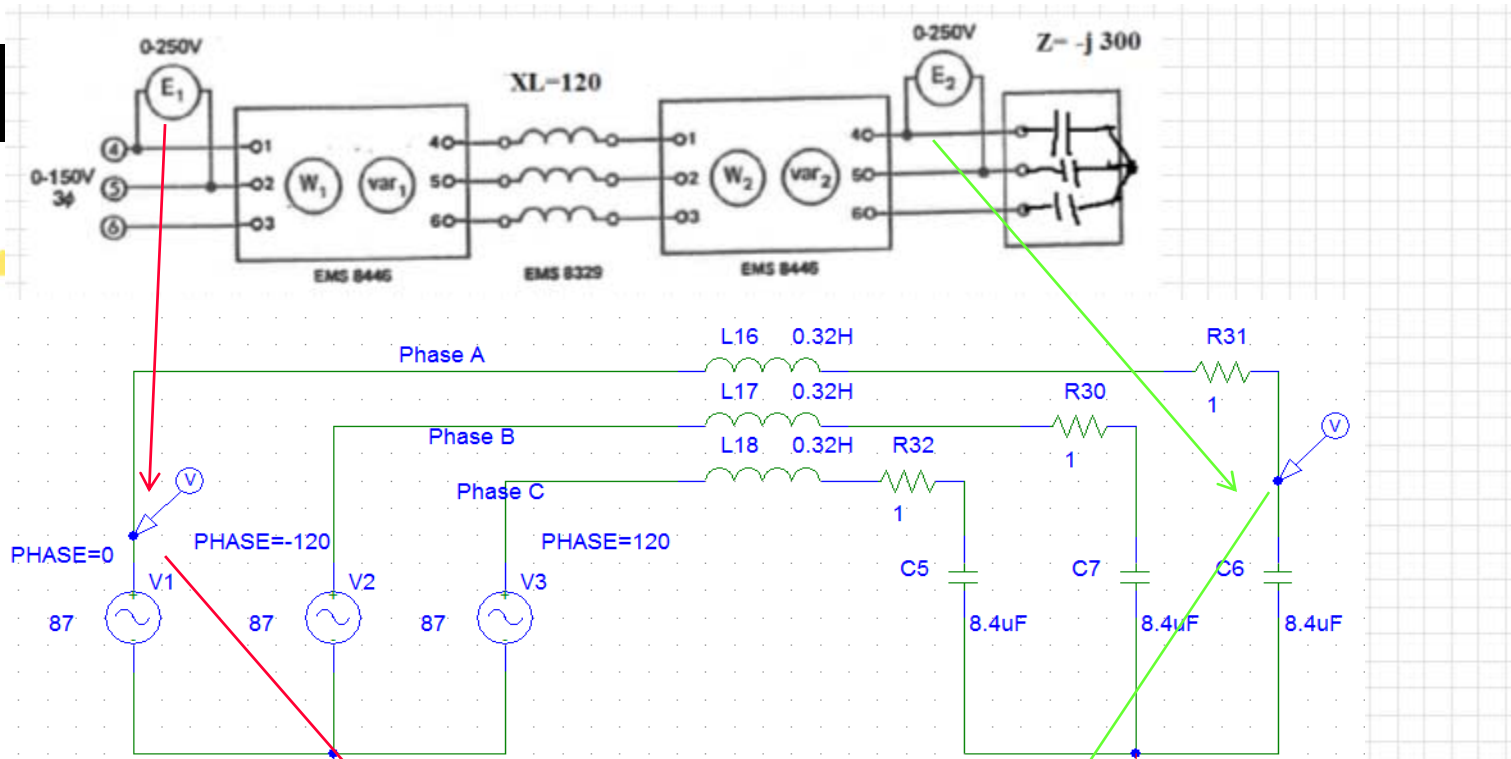


$$\begin{aligned}
 V_L &= 150 & V_P &= \frac{V_L}{\sqrt{3}} = 86.60254 & Z_{tr} &= 0 + i \cdot 120 & Z_{load} &= (-i) \cdot 300 = -300i \\
 Z &= Z_{tr} + Z_{load} & Z &= -180i & I_L &= \frac{V_P}{Z} = 0.481125i \\
 \theta_v &= \arg(V_P) = 0 & \theta_i &= \arg(I_L) = 1.570796 & \theta &= \theta_v - \theta_i = -1.570796 \\
 P_{tot} &= 3 \cdot |V_P| \cdot |I_L| \cdot \cos(\theta) = 4.364354 \cdot 10^{-13} \\
 Q_{tot} &= 3 \cdot |V_P| \cdot |I_L| \cdot \sin(\theta) = 125 \\
 S_{tr} &= 3 \cdot |I_L|^2 \cdot Z_{tr} = 83.333333i & P_{tr} &= \operatorname{Re}(S_{tr}) = 0 & Q_{tr} &= \operatorname{Im}(S_{tr}) = 83.333333 \\
 S_{load} &= 3 \cdot |I_L|^2 \cdot Z_{load} = -208.333333i & P_{load} &= \operatorname{Re}(S_{load}) = 0 & Q_{load} &= \operatorname{Im}(S_{load}) = -208.333333
 \end{aligned}$$

Voltage Regulation

$$\begin{aligned}
 V_{load} &= I_L \cdot Z_{load} = 144.337567 & |V_{load}| &= 144.337567 \\
 \frac{|V_P| - |V_{load}|}{|V_P|} \cdot 100 &= 66.666667 \text{ percent}
 \end{aligned}$$

Example



Experimentation Setup

